## Theory of structure

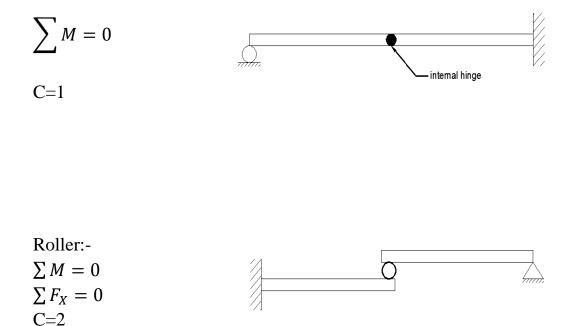
Stability and determinacy of structures

Beams

✤ Total equation of equilibrium of beam

$$\sum F_X = 0$$
$$\sum F_Y = 0$$
$$\sum M = 0$$

 Equation of condition Internal hinge:-

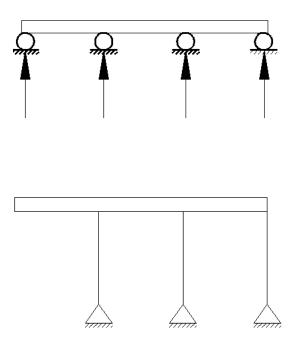


Let r= No. of reaction

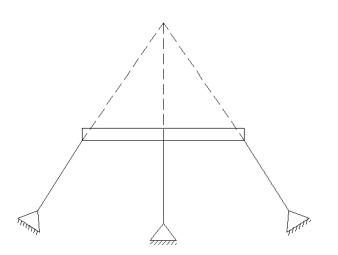
1- If r < c+3, unstable

- 2- r=c+3, determine if stable
- 3- r> c+3, indeterminate if stable Let (m) degree of indeterminate m= r- (c+3)

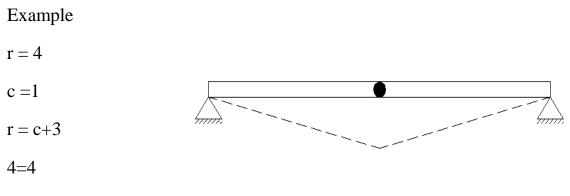
- $\boldsymbol{\diamondsuit}$  the structure is said to be unstable if one of the following facts couter
  - 1- r< c+3
  - 2- The reaction element constitutes a parallel force system.



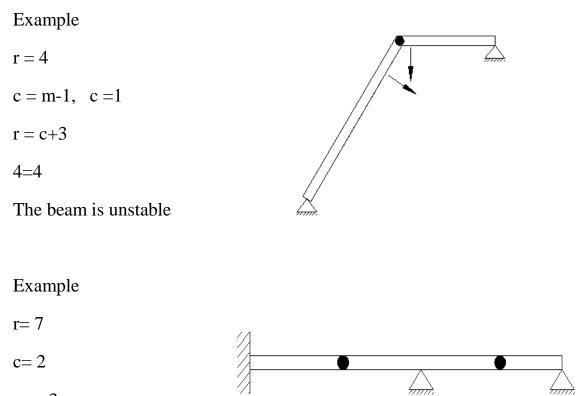
3- The reaction element constitutes a concurrent force system.



4- Internal geometric instability:-



The beam is unstable because the Internal geometric instability

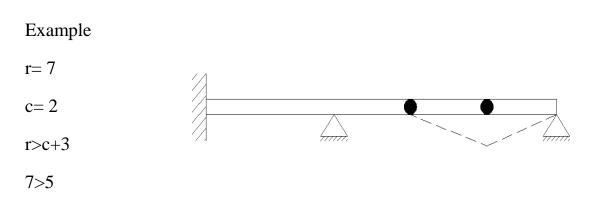


3

r>c+3

7>5

The beam is indeterminate 2<sup>nd</sup> degree if stable



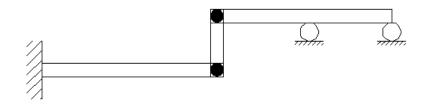
The beam is unstable

Examples:-

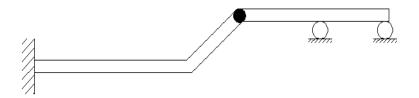
Beam	r	c	c+3	state	Stability & determinate.
india India	3	0	3	r=c+3	Stable & deter.
	4	0	3	r>c+3	Stable & indeter. First degree
Anna Anna	6	1	4	r>c+3	Stable &indeter. Second degree
man, bank bank	6	2	5	r>c+3	unstable
anan antan antan	3	0	3	r =c+3	unstable

#### Home Works

H.W1: Find the stability and determinacy of beam.



H.W2: Find the stability and determinacy of beam.



Stability and Determinacy of Trusses

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b + r = unknown
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- j = equations
- 1- b + r < 2j, the truss is unstable
- 2- b + r = 2j, the truss is determinate if stable
- 3- b + r > 2j, the truss is indeterminate if stable

Let (m) equal to the degree of indeterminate m=(b+r)-2j

b = No. of bars

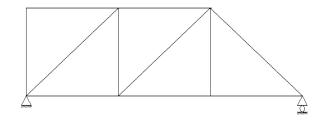
- r = No. of reactions
- j = No. of joints

5

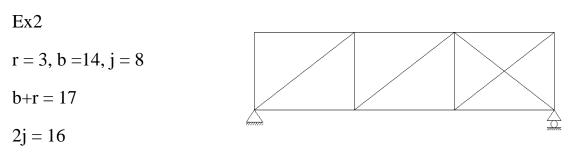
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**Examples:** - Find the stability and determinacy of trusses below.

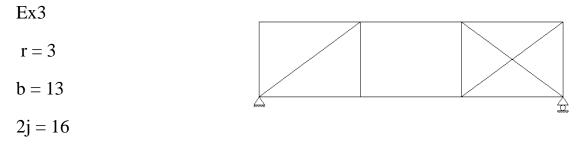
Ex1 r = 3, b = 11, j = 7 b+r = 14 2j= 14b+r = 2j



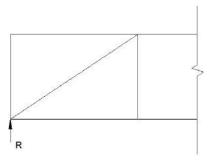
The truss is stable & determinate



b+r > 2j, the truss is stable indeterminate  $1^{st}$  degree

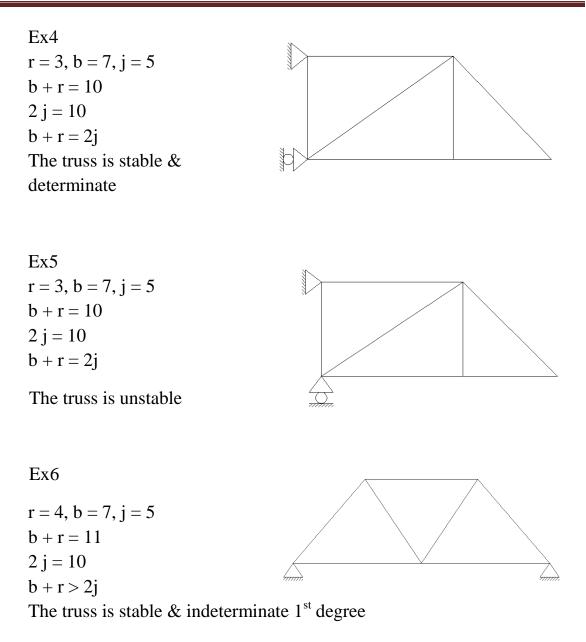


b+r = 2j, the truss is unstable because of  $\sum F_y \neq 0$ , in this section



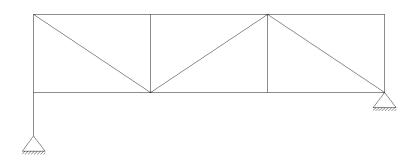
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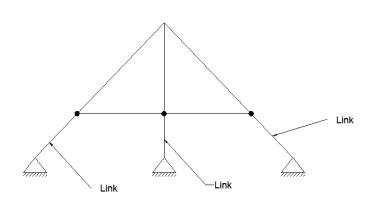
### Home works

H.W1



7

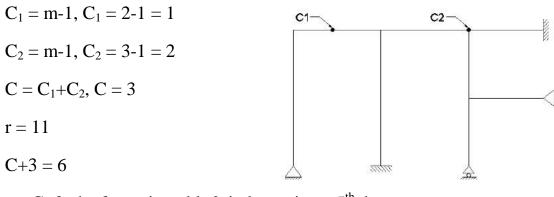
H.W2



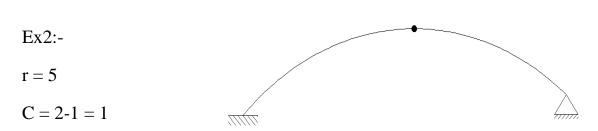
### Stability and Determinacy of Frames

- 1- Open frames
- r < C+3, unstable
- r = C+3, determinate if stable
- r > C+3, indeterminate if stable

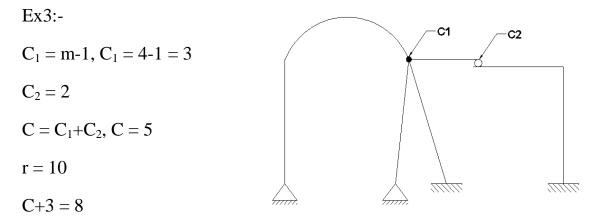
Ex1:- Find the stability and determinacy of frame below



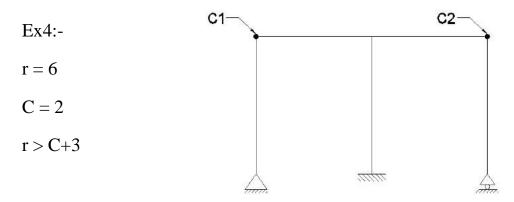
r > C+3, the frame is stable indeterminate 5<sup>th</sup> degree.



r > C+3, the frame is stable & indeterminate 1<sup>st</sup> degree.



r > C+3, the frame is stable & indeterminate  $2^{nd}$  degree.



The frame is unstable because of internal geometric instability

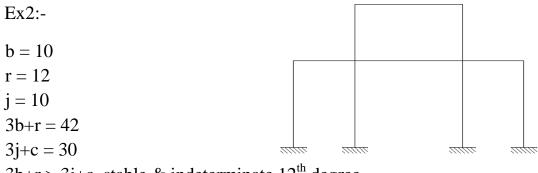
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#### 2- Closed Frames:-

3b+r < 3j+c, unstable 3b+r = 3j+c, determinate if stable 3b+r > 3j+c, indeterminate if stable

Where, 3b+r = unknown 3j+c = equations b = No. of members r = No. of reactions j = No. of joints

Ex1: b = 10 r = 9 j = 9 3b+r = 39 3j+c = 273b+r > 3j+c, stable & indeterminate  $12^{th}$  degree



3b+r > 3j+c, stable & indeterminate  $12^{th}$  degree

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Ex3:-		
b = 4		
b = 4 r = 6		
j = 4       c = 0		
$\mathbf{c} = 0$		
3b+r = 18	where the second s	uhu.
3j+c = 12		
3b+r > 3j+c, stable & indeter	minate 6 <sup>th</sup> degree	

Ex4:-

b = 9 r = 5 j = 7  $c = m-1 \Longrightarrow c = 1$  3b+r = 31 3j+c = 22 $3b+r > 3j+c, \text{ stable & indeterminate 9}^{\text{th}} \text{ degree}$ 

Ex5:-

b = 10 r = 9 j = 9  $c = m-1 \Longrightarrow c = 4-1 \Longrightarrow c = 3$  3b+r = 393j+c = 30

3b+r > 3j+c, stable & indeterminate  $9^{th}$  degree

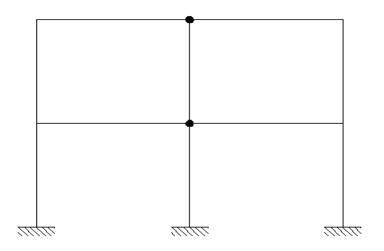
ملاحظة:- اذا جاء ال internal hinge في بداية او نهاية الضلع فيحسب منه (c &j) اما اذا جاء في داخل الضلع فيحسب منة c فقط

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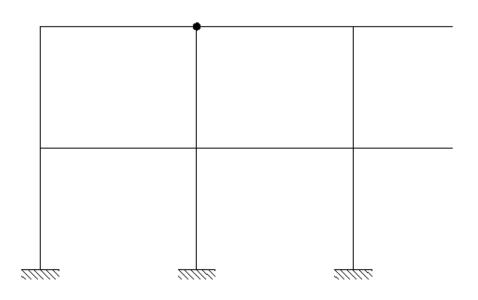
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Home work:

H.W1: Find the stability and determinacy of frame below



H.W2: Find the stability and determinacy of frame below



Unknowns	Equations		
1- Each truss member give one unknown	<ul><li>1- each member carry moment give</li><li>(3 equations)</li></ul>		
2- reactions	2- each joint connect truss members only give (2 equations)		
3- each joint connect member carry moment give unknown in these equation (2*(m-1))			

# Stability and Determinacy of Composite Structure

Ex1:- Find the stability and determinacy of composite structure as shown below.

Solution:

Equations

(3\*3) + 0 = 9

Unknowns

1+3+(3\*(2(2-1))) = 10

Unknowns > Equations, Stable & indeterminate 1<sup>st</sup> degree

Ex2:- Find the stability and determinacy of composite structure as shown below.

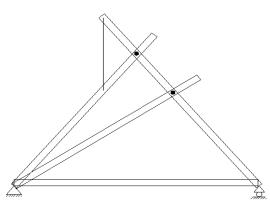
Solution:

Equations

(4\*3) + 0 = 12

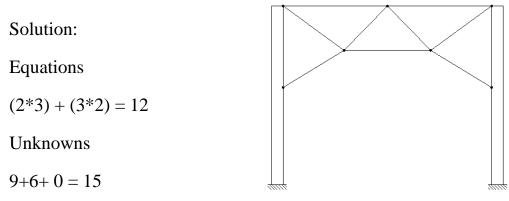
Unknowns

1+3+(3\*(2(2-1)))+(2(3-1)) = 14



Unknowns > Equations, Stable & indeterminate  $2^{nd}$  degree

Ex3:- Find the stability and determinacy of composite structure as shown below.



Unknowns > Equations, Stable & indeterminate  $2^{nd}$  degree

Ex4:- Find the stability and determinacy of composite structure as shown below.

Solution:

Equations

(1\*3) + (7\*2) = 17

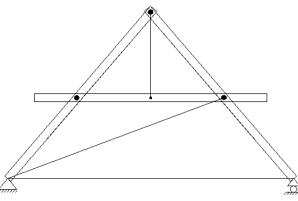
Unknowns

13+5+0 = 18

Unknowns > Equations, Stable & indeterminate 1<sup>st</sup> degree

H.w: Find the stability and determinacy of composite structure as shown below.

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